

Lecture 10

Deterministic Finite Automata

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Troy Vasiga et al
University of Waterloo

Review

- ▶ formal languages give a theoretical basis for communication and organizing processes
- ▶ terminology (alphabet, word, language)
- ▶ specification vs. recognition
- ▶ studying language levels that increase in power/complexity
- ▶ a language is regular if there exists a DFA that specifies/recognizes it

DFAs

- ▶ a.k.a. finite state machines
- ▶ start state
- ▶ final/accepting states
- ▶ implicit error state
- ▶ accepted and rejected words
- ▶ $L(M)$ – the language recognized by DFA M
- ▶ Notice that $L(M) = L(M')$ even though $M \neq M'$

Formal Definition

A DFA is a 5-tuple $(\Sigma, Q, q_0, A, \delta)$ where

- ▶ finite alphabet Σ
- ▶ finite set of states Q
- ▶ start state q_0
- ▶ set of final/accepting states $A \subseteq Q$
- ▶ transition function: $\delta : Q \times \Sigma \rightarrow Q$

DFA Interpreter

Input: A word $w = w_1w_2\dots w_n$

Output: true if accepted, false if rejected

Implementing DFAs

Need to implement the transition function somehow

NFAs

- ▶ $L = \{bba, baa, bbaa, bbbaa, bbbbaa, \dots\}$ which is either 2 b's followed by an a, or 1 or more b's followed by 2 a's
- ▶ try to derive this using a DFA
- ▶ a nice NFA?

NFA definition

Same as a DFA with the following change:

$$T : Q \times \Sigma \rightarrow 2^Q$$

That is, we can be in a set of states, and thus T is a *relation* instead of a function.

NFA interpreter

Implementing an NFA interpreter

Differences between NFAs and DFAs

Transducers

Add an output alphabet, and each transition can output a single character from that output alphabet.