



Organizing principles in networking

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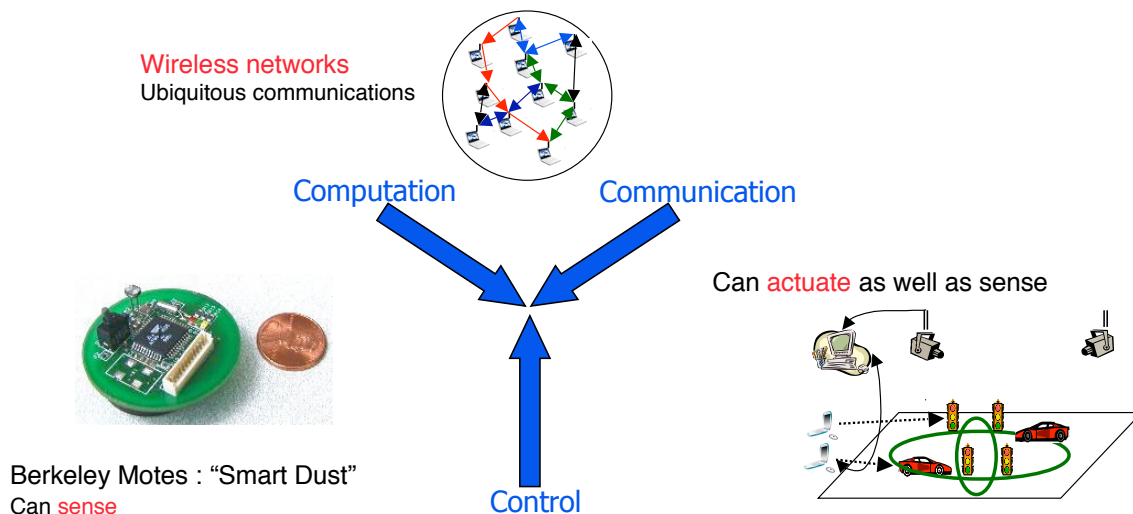
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From wireless to sensor networks and control



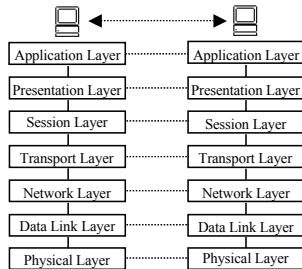
- ◆ Interaction with the physical world through sensing and actuation
 - Convergence of Control with Communication and Computation

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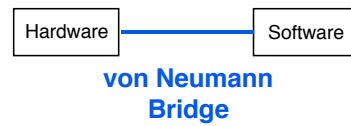


Architecture and abstractions

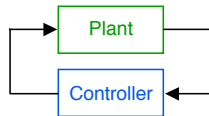
OSI



Serial computation



Control systems



Digital Communication

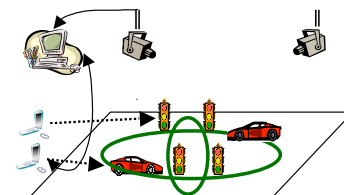
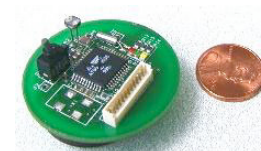
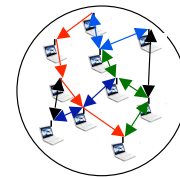


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Outline of talk

- ◆ Wireless networks
 - How to organize data transfer
- ◆ Sensor networks
 - Theory for in-network processing
- ◆ Convergence with control
 - Middleware and multi-technology integration



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Capacity and Architecture of Wireless Networks

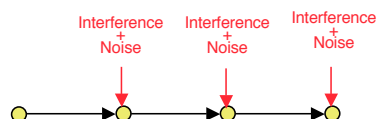
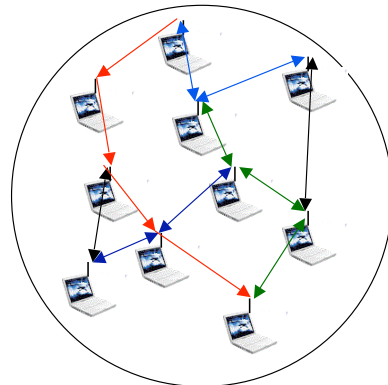
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Ad Hoc Wireless Networks

- ◆ Communication networks formed by nodes with radios
 - Ad Hoc Wireless Networks

- ◆ Current proposal for operation:
 - Multi-hop transport
 - Nodes relay packets until they reach their destinations
 - Fully decode packets at each stage treating all interference as noise

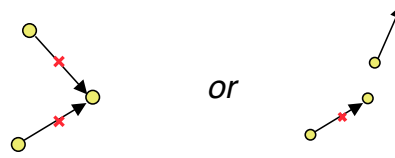


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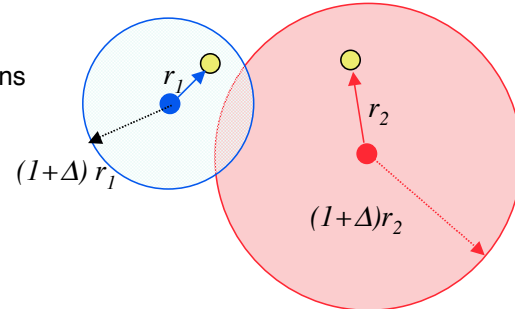
When all interference is regarded as noise ...

- ◆ Packets can collide destructively



- ◆ Several Models

- Reception is successful if
 - » Receiver not in vicinity of two transmissions



» Or SIR Ratio = $\frac{P_i r_i^{-\alpha}}{N + \sum_{j \neq i} P_j r_j^{-\alpha}} \geq \beta$

» Or Rate depends on SIR: Rate = $B \log \left(1 + \frac{P_i r_i^\delta}{N + \sum_{j \neq i} P_j r_j^\delta} \right)$ bps

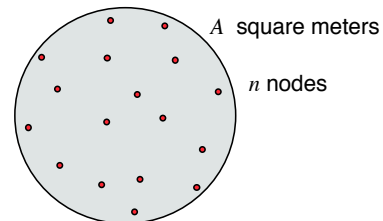
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Scaling laws under interference model

- ◆ Theorems (Gupta & K 2000)

- Disk of area A square meters
- n nodes
- Each can transmit at W bits/sec
- Packets interfere/collide with each other



- ◆ Best Case: Network can transport $\Theta(W\sqrt{An})$ bit-meters/second

- ◆ Square root law

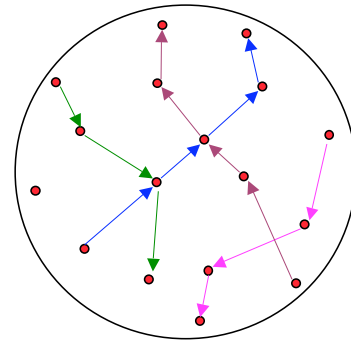
- Transport capacity doesn't increase linearly, but only like square-root
- Each node gets $\frac{c}{\sqrt{n}}$ bit-meters/second

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Random Network Scenario

- ◆ n nodes randomly located in disk of unit area
 - Each node chooses random destination
 - Equal throughput λ bits/sec for all OD pairs
 - Each node chooses same range r



- ◆ Each node can send $\Theta\left(\frac{1}{\sqrt{n \log n}}\right)$ bits/sec even with
 - With best choice of spatio-temporal scheduling, ranges and routes

- ◆ Definition of capacity

$$\lim_{n \rightarrow \infty} \Pr(\lambda(n) = \frac{c}{\sqrt{n \log n}} \text{ is feasible}) = 1, \text{ and}$$

$$\lim_{n \rightarrow \infty} \Pr(\lambda(n) = \frac{c'}{\sqrt{n \log n}} \text{ is feasible}) = 0$$

Sharp cutoff phenomenon

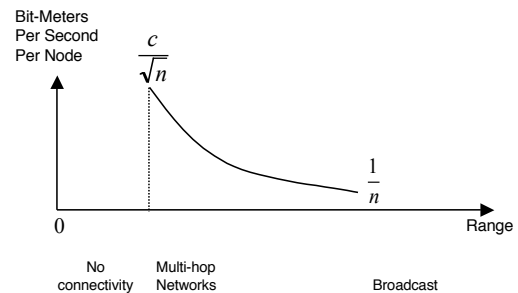
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Order optimal operation under “collision” model

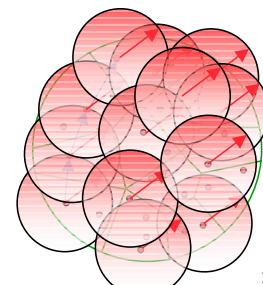
- ◆ Optimal operation is multi-hop

- Transport packets over many hops of distance $\frac{c}{\sqrt{n}}$



- ◆ Optimal multi-hop architecture

- Group nodes into cells of size $\log n$
- Choose a common power level for all nodes
 - » Nearly optimal
- Power should be just enough to guarantee network connectivity
 - » Sufficient to reach all points in neighboring cell
- Route packets along nearly straight line path from cell to cell



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But are these fundamental limits?

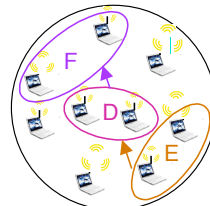
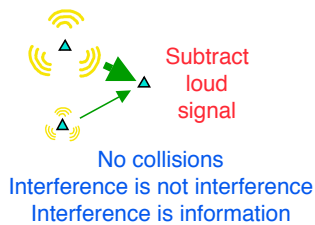
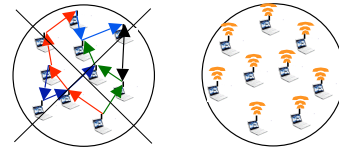
Is this the right architecture for data transfer?

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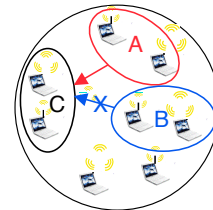


Wireless networks are not wired networks ...

- ◆ Wireless networks are formed by nodes with radios
 - Maxwell rather than Kirchoff
- ◆ Nodes can cooperate in many complex ways



Signal
Interference + Noise
↑
Reduce by cancellation



“There are more things in heaven and earth, Horatio,
Than are dreamt of in your philosophy.”
— Hamlet

Goal

- ◆ A strategic theory to determine basic architecture
- ◆ Specify what functionalities needed
- ◆ Then develop protocols to implement the architecture

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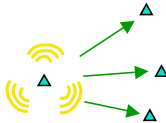
Network information theory

- ◆ Shannon's original work was for a single link

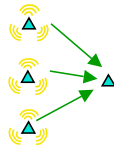


Triumphs

Gaussian broadcast channel



Multiple access channel

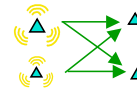


Unknowns

The simplest relay channel



The simplest interference channel



- ◆ Networks being built (ad hoc networks, sensor nets) are much more complicated

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Model of system: A planar network

- ◆ Introduce node locations, distances between nodes, and attenuation as a function of distance

- ◆ n nodes in a plane

- ◆ ρ_{ij} = distance between nodes i and j

- ◆ Minimum distance ρ_{\min} between nodes

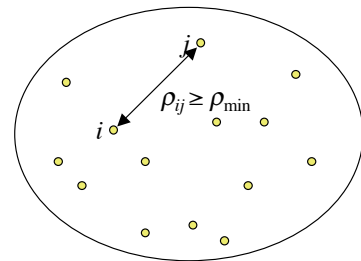
- ◆ Signal attenuation with distance ρ : $\frac{e^{-\gamma\rho}}{\rho^\delta}$

- $\gamma \geq 0$ is the absorption constant

- » Generally $\gamma > 0$ since the medium is absorptive unless over a vacuum

- » Corresponds to a loss of $20\gamma \log_{10} e$ db per meter

- $\delta > 0$ is the path loss exponent



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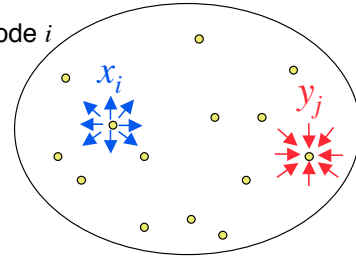
Transmitted and received signals

- ◆ W_i = symbol from some alphabet $\{1, 2, 3, \dots, 2^{TR_{ik}}\}$ to be sent by node i

- ◆ $x_i(t) = f_{i,t}(y_i^{t-1}, W_i)$ = signal transmitted by node i time t

- ◆ $y_j(t) = \sum_{\substack{i=1 \\ i \neq j}}^n \frac{e^{-\gamma \rho_{ij}}}{\rho_{ij}} x_i(t) + z_j(t)$ = signal received by node j at time t

$N(0, \sigma^2)$



- ◆ Destination j uses the decoder $\hat{W}_i = g_j(y_j^T, W_j)$

- ◆ Error if $\hat{W}_i \neq W_i$

- ◆ (R_1, R_2, \dots, R_L) is feasible rate vector if there is a sequence of codes with

$$\text{Max}_{W_1, W_2, \dots, W_L} \Pr(\hat{W}_i \neq W_i \text{ for some } i \mid W_1, W_2, \dots, W_L) \rightarrow 0 \text{ as } T \rightarrow \infty$$

- ◆ **Individual power constraint** $P_i \leq P_{ind}$ for all nodes i . **or Total power constraint** $\sum_{i=1}^n P_i \leq P_{total}$

- ◆ **Transport Capacity** $C_T = \sup_{(R_1, R_2, \dots, R_{n(n-1)})} \sum_{i=1}^{n(n-1)} R_i \cdot \rho_i$ bit-meters/second or bit-meters/slot

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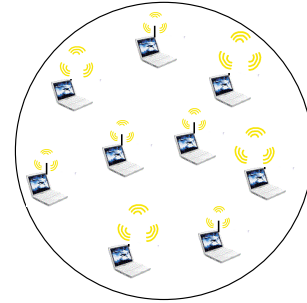
The Results



Power cost of transport capacity

◆ Theorem: Bit-meters per Joule bound (Xie & K'02)

- Suppose $\gamma > 0$, there is some absorption,
- Or $\delta > 3$, if there is no absorption at all
- Then for all Planar Networks



$$C_T \leq \frac{c_1(\gamma, \delta, \rho_{\min})}{\sigma^2} \cdot P_{total}$$

where

$$c_1(\gamma, \delta, \rho_{\min}) = \frac{2^{2\delta+7} e^{-\rho_{\min}/2} (2 - e^{-\rho_{\min}/2})}{\gamma^2 \rho_{\min}^{2\delta+1} (1 - e^{-\rho_{\min}/2})} \quad \text{if } \gamma > 0$$

$$= \frac{2^{2\delta+5} (3\delta - 8)}{(\delta - 2)^2 (\delta - 3) \rho_{\min}^{2\delta-1}} \quad \text{if } \gamma = 0 \text{ and } \delta > 3$$

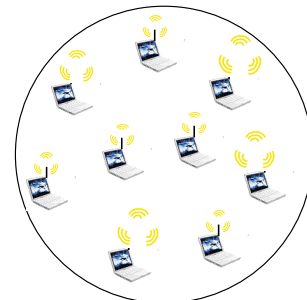
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O(n) upper bound on Transport Capacity

◆ Theorem: Transport capacity is O(n) (Xie and K'02)

- Suppose $\gamma > 0$, there is some absorption,
- Or $\delta > 3$, if there is no absorption at all
- Then for all Planar Networks



$$C_T \leq \frac{c_1(\gamma, \delta, \rho_{\min}) P_{ind}}{\sigma^2} \cdot n$$

- ◆ Same as square root law based on treating interference as noise
 - $\Theta(\sqrt{An}) = \Theta(n)$ since area A grows like $\Omega(n)$

- ◆ So multi-hop with decode and forward with interference treated as noise is order optimal architecture whenever $\Theta(n)$ can be achieved { No need for network coding, multi-user detection, etc. 18 / 51



From scaling laws to architecture

- ◆ Explicitly incorporated *distance* in model
 - » Distances between nodes
 - » Attenuation as a function of distance
 - » Distance is also used to measure transport capacity

- ◆ Studied networks with *arbitrary numbers of nodes*

- ◆ Make progress by asking for less
 - Instead of studying capacity region, study the *transport capacity*
 - Instead of asking for exact results, study the *scaling laws*
 - » The exponent is more important
 - » The preconstant is also important but is secondary - so bound it
 - Draw some broad conclusions about *order-optimal architecture*
 - » Optimality of multi-hop when absorption or large path loss
 - » Optimality of coherent multi-stage relaying with interference cancellation when no absorption and very low path loss

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What about pre-constants?

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From pre-constants to architecture: Ideas for protocol design

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Traffic adaptive routing: STARA

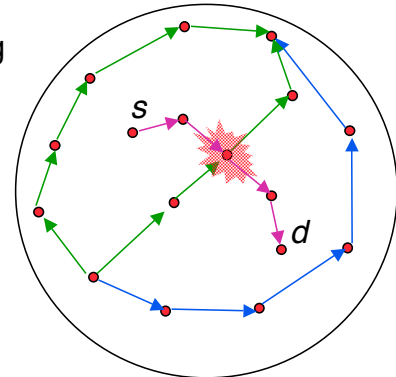
(Gupta & K 1998,
Borkar & K 2003,
Raghunathan & K 2004)

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Traffic adaptive routing protocols

- ◆ Routing protocol based on Minimum Hop routing
- ◆ However Min Hop paths can mutually interfere
- ◆ Moreover we may want to use multiple paths
- ◆ How to quantify the possible improvement in the preconstant?



- ◆ Few Sources Theorem: A 4x improvement (Raghunathan & K '04)

- If Number of sources = $o(n^{1/6})$
- There exist flow avoiding, multiple paths so that

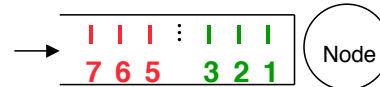
$$\liminf_{n \rightarrow \infty} \frac{\text{Thpt of Flow Avoiding Multipath routing}}{\text{Throughput of Minimum Hop Routing}} \geq 4$$

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Delay Equalizing solution

- ◆ And we may want low delay



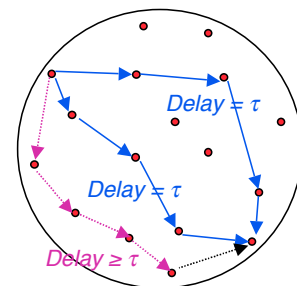
- ◆ Goal: Route traffic from origin to destination such that

- All **utilized** routes have the **same** mean delay
- All **unutilized** routes have **larger** mean delay

The Wardrop equilibrium:

“The journey times on all the routes actually used are equal, and less than those which would be experienced by a single vehicle on any unused route.”

J. G. Wardrop, “Some Theoretical Aspects of Road Traffic Research,” *Proc. Inst. Civil Engineers, Part 2*, pp. 325-378, 1952.



- ◆ Delay Estimation Algorithm

- D_{ij}^d = Estimate of delay from i to d via j
- $D_{ij}^d(\text{new}) = (1-\theta) D_{ij}^d(\text{old}) + \theta (\text{Latest } D_{ij}^d)$
- D_i^d = Average i to d delay over *all* routes
- $D_i^d(\text{new}) = \sum_j p_{ij}^d(\text{new}) D_{ij}^d(\text{new})$

- ◆ Route Adaptation Algorithm

- p_{ij}^d = Proportion of traffic from i to d routed via j
- $p_{ij}^d(\text{new}) = p_{ij}^d(\text{old}) + \alpha p_{ij}^d(\text{old}) (D_i^d(\text{new}) - D_{ij}^d(\text{new}))$
- Note: Subtraction eliminates clock offsets!
- Also we are equalizing delays!

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The COMPOW Protocol for Power Control

(Narayanaswamy, Kawadia, Sreenivas & K '00)

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Power Control problem: How to choose transmissions power levels?

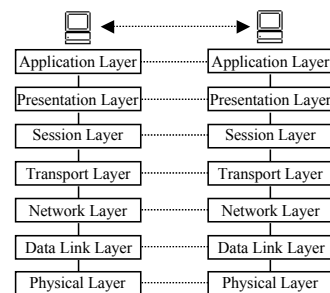
- ◆ Conceptualization problem: Which Layer?
 - Physical layer: Quality of reception
 - Network layer: Impact on routing
 - Transport layer: Higher power impacts congestion

- ◆ COMPOW Solution
 - All nodes use common power chosen just large enough for network connectivity - or larger

$$\text{Distance-rate product} \approx r \times \frac{1}{r^2} = \frac{1}{r}$$

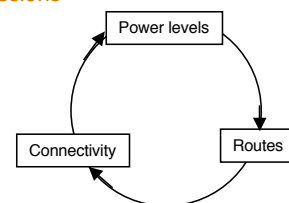
Transmission range

Number of simultaneous transmissions



- ◆ This is a Network Layer problem
 - Interdependence of Power Control, Routing, Connectivity

- ◆ So joint solution for Power Control and Routing situated at the Network Layer



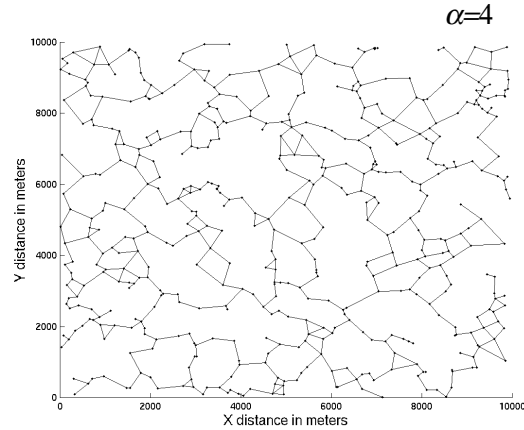
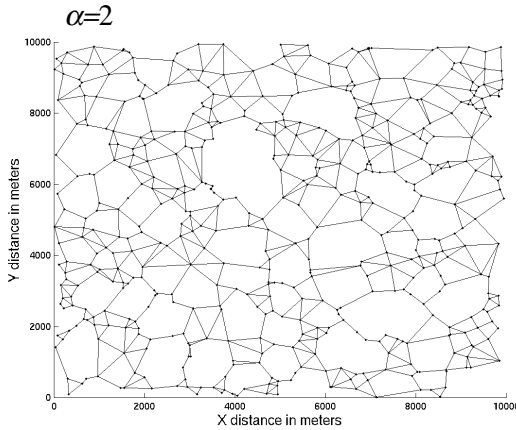
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Low common power level also yields transmission power efficient routes

◆ Theorem

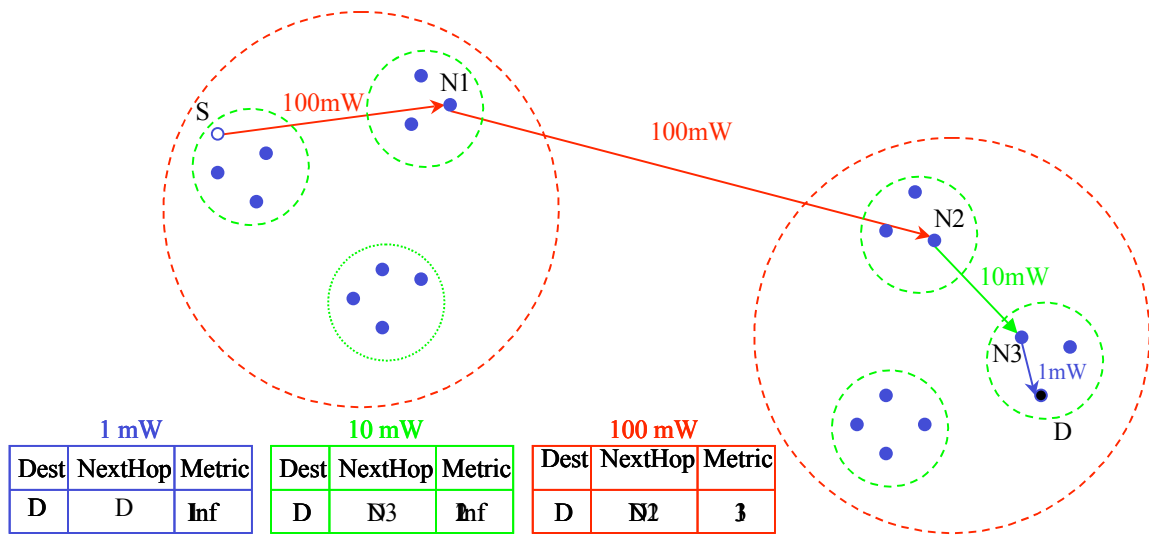
- For propagation path loss $1/\rho^\alpha$ with $\alpha \geq 2$ the minimum power routes give a planar graph with straight line edges that do not cross.
- The graph for $\alpha > 2$ is a subgraph of that for $\alpha = 2$.



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Routing Table at N2



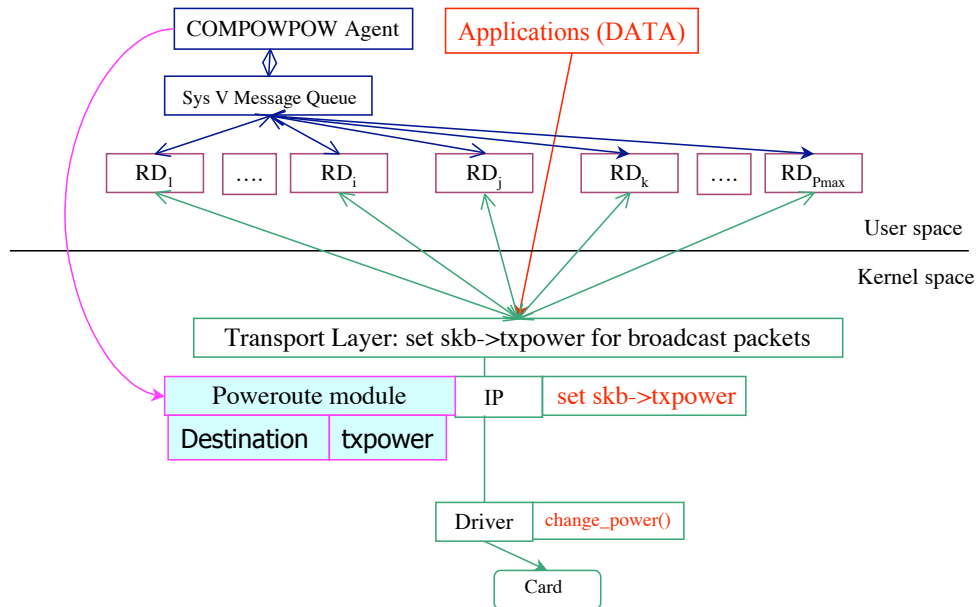
1 mW			10 mW			100 mW		
Dest	NextHop	Metric	Dest	NextHop	Metric	Dest	NextHop	Metric
D	D	Inf	D	N3	Inf	D	N2	3

Kernel IP Routing Table

	Dest	NextHop	Metric	TxPower
N2	D	N3	3	100mW



Software Architecture for Power Control: COMPOW



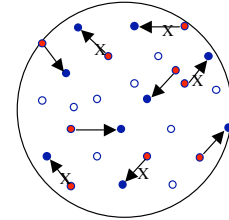
The SEEDEX Protocol for Media Access Control

(Rozovsky & K 2000)

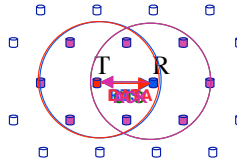


The Media Access Control problem

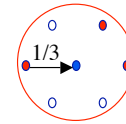
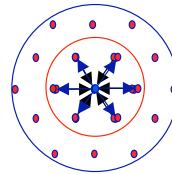
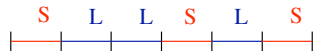
- ◆ Wireless is a shared medium
 - Neighbors of receiver should not transmit
 - Circular problem: Communication \leftrightarrow Coordination
 - How to resolve in asynchronous distributed real time fashion?



- ◆ IEEE 802.11 solution
 - Two neighborhoods silenced
 - Backoff
 - Wasteful?



- ◆ SEEDEX Solution
 - Random Bernoulli schedule: $p, 1-p$



- Seed Exchange with two hop neighbors

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Sensor Networks: Towards a theory of in-network processing

(Giridhar & K 2004)

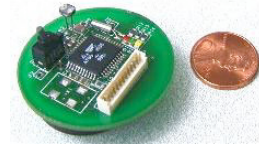
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The oncoming convergence: Harvesting statistics from sensor networks

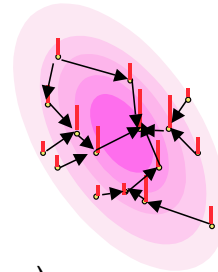
- ◆ Sensor networks

- Example: Berkeley Motes
 - » Can **sense**, wirelessly communicate, compute



- ◆ Examples of Tasks

- Environmental monitoring
 - » n nodes take temperature measurements x_1, x_2, \dots, x_n
 - » Determine the Mean temperature: $(x_1 + x_2 + \dots + x_n)/n$
- Alarm networks
 - » Determine the Max temperature: $\text{Max } x_i$



- ◆ More generally: Consider a symmetric function $F(x_1, x_2, \dots, x_n)$

- Eg. Max, Mean, Mode, Median, Percentile, Frequency Histogram

- ◆ How should we **process information in-network** to compute and collect functions of interest?

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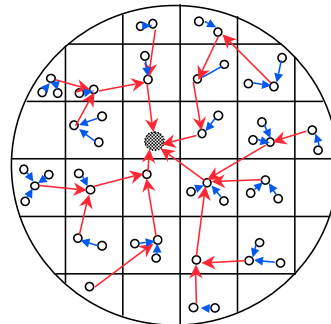
Computing symmetric functions: Harvesting the *type* (Giridhar & K '03)

- ◆ Value of symmetric function depends only on the *type* of the measurement set

- *Type* = Frequency histogram

- ◆ Theorem: The maximum frequency at which types can be harvested at a fusion node in a random multihop network is $\Theta(\frac{1}{\log n})$

- Strategy
 - » Tessellate
 - » Fuse locally
 - » Compute along a rooted tree of cells



- ◆ Different architecture for “Max” function

- Block coding

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Summary: Order of difficulty of computations

$\Theta(1/n)$

Collocated network:
Mean, Mode, Type

*Data
downloading*

$\Theta(1/\log n)$

Random planar network:
Mean, Mode, Type

Collocated network:
Max

$\Theta(1/\log \log n)$

Random planar network
Max

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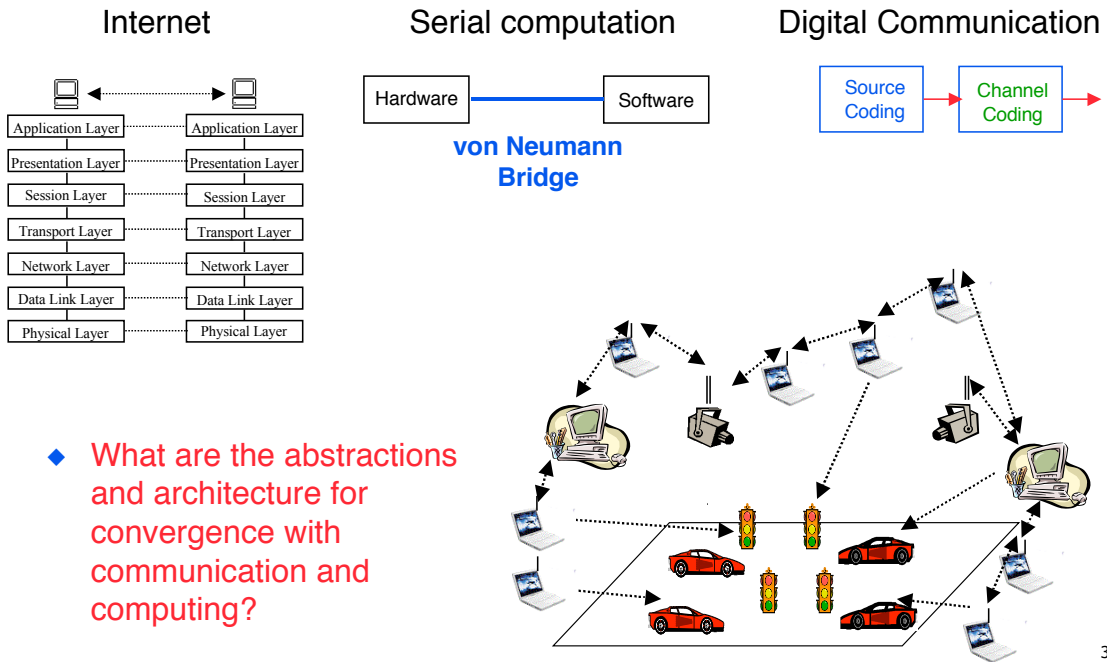
The convergence of control with communication and computing

(Graham & K '03,04, Baliga & K '03, Giridhar & K '03, Huang, Graham & K '03, Graham, Baliga & K '04)

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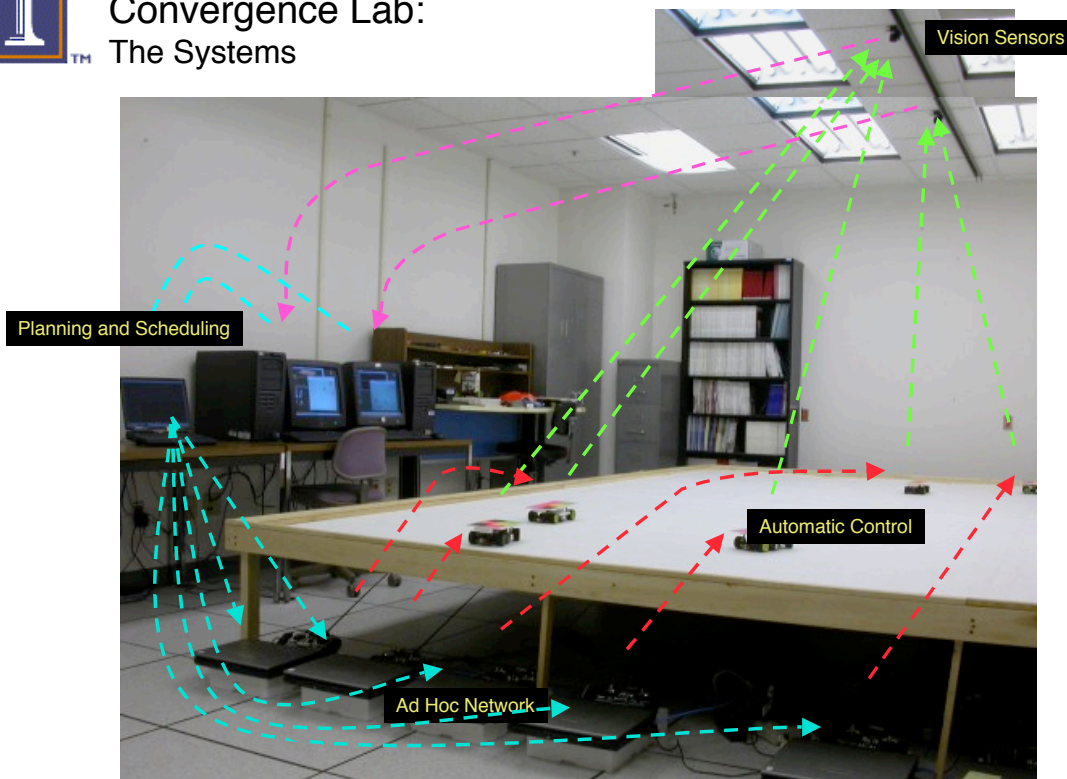
Challenge of architecture and abstractions for convergence



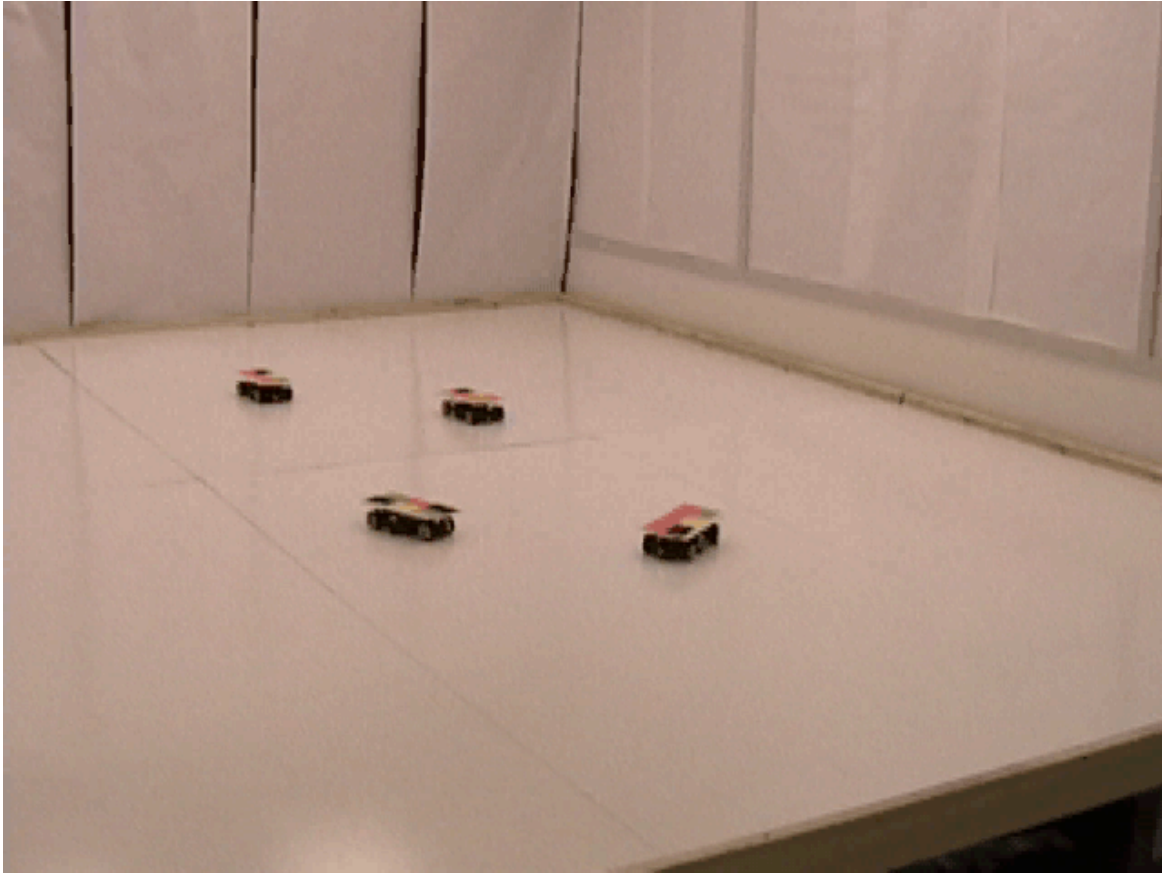
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Information Technology Convergence Lab: The Systems



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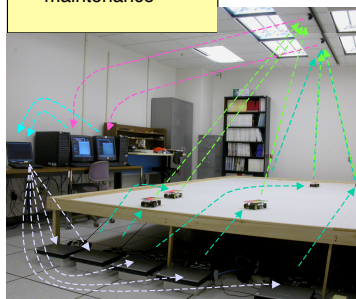
Subsystems

- Control law development
- Time scale decomposition
 - State estimation
 - Asynchronous measurement
 - Lossy measurement
 - Sensor errors
 - Robustness
 - Vision based control

- Distributed application development
- Feature bloat environment
 - Rapid
 - Reliable
 - Evolvable

- Optimizing at run-time
- On-line identification and adaptation
 - Reactive planning and scheduling
 - Migration for communication vs. computation load balancing

- System integration
- Hardware development
 - Software development
 - System maintenance



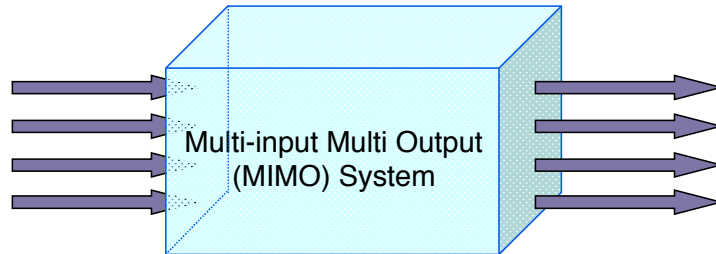
- Subsystems
- Ad hoc wireless network
 - Cisco Aironet 802.11b pcmcia cards
 - Vision and sensor network
 - Matrox Imaging frame grabber and library
 - Planning and scheduling
 - Centralized and distributed
 - Predictive controller

- Software
- Middleware
 - Services

- Measuring and managing time in a distributed system
- Measurement latencies
 - Clock synchronization
 - System performance related to timing accuracies

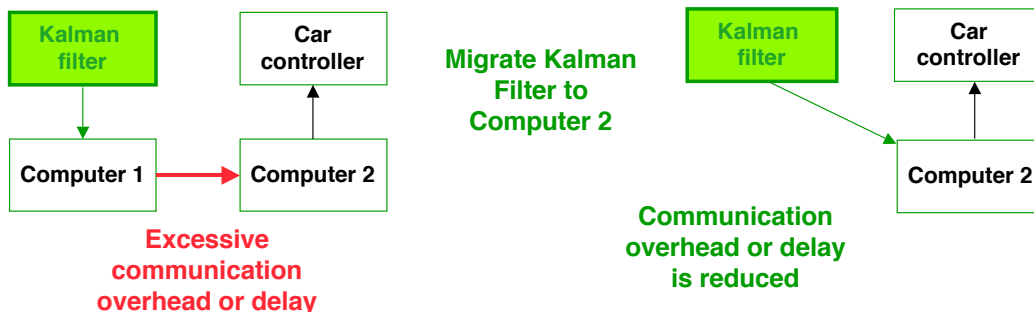
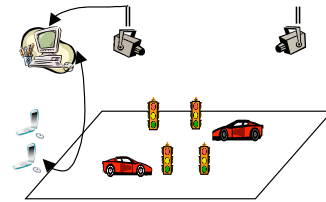


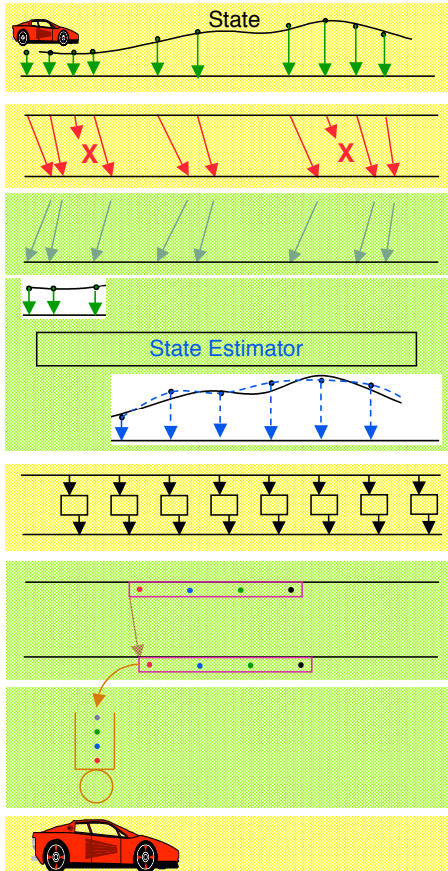
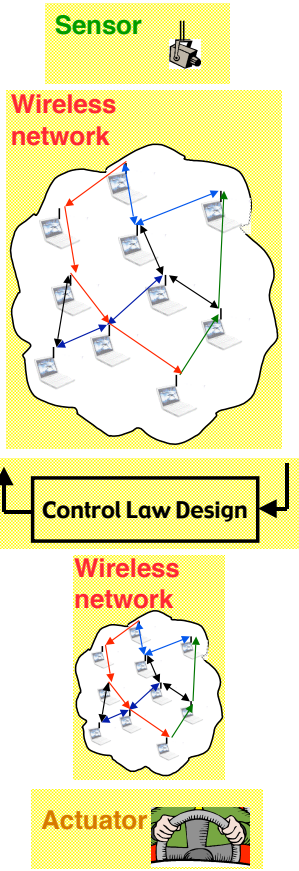
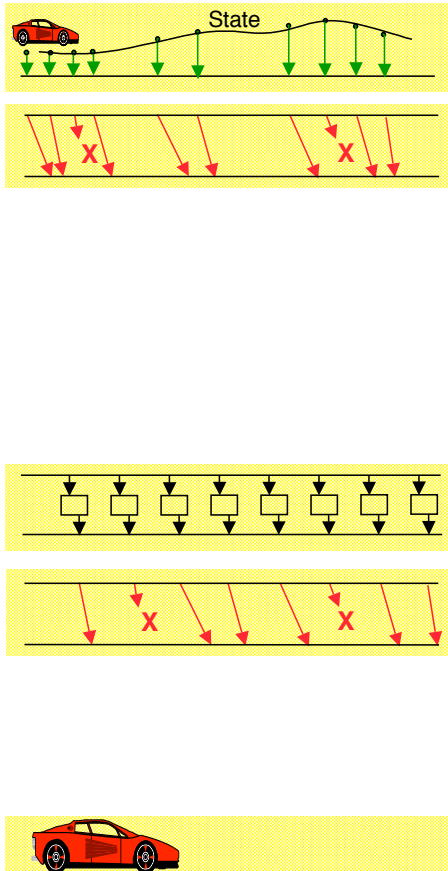
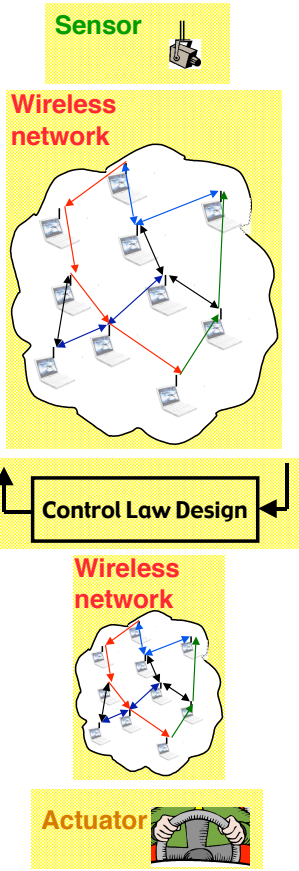
Abstraction of virtual collocation



Middleware: EtherArch Software (Baliga & K'03)

- ◆ Component architecture
- ◆ Location independence
- ◆ Semantic addressing of components
- ◆ System startup and upgrade during execution
- ◆ Time translation
 - Knowledge of per-packet delay important for control
- ◆ Automatic migration of components for performance



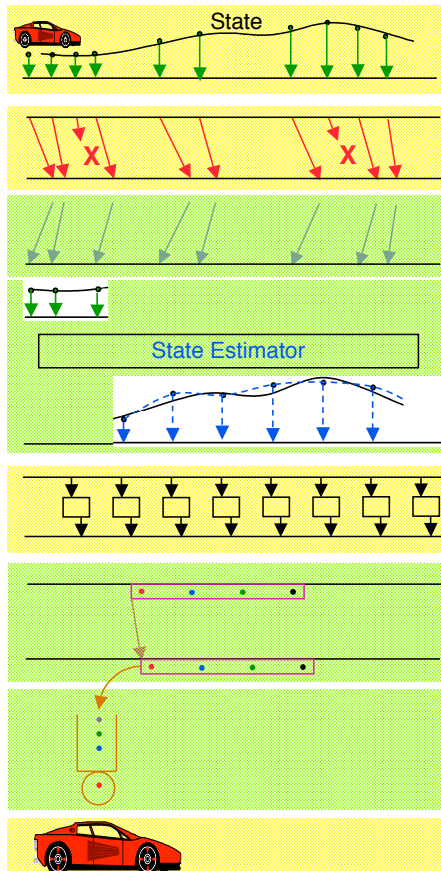
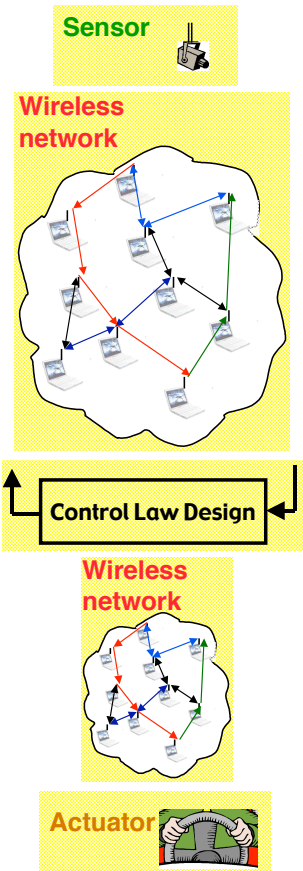


Time Translation Service

State Estimator

Receding Horizon Control

Actuator Buffer

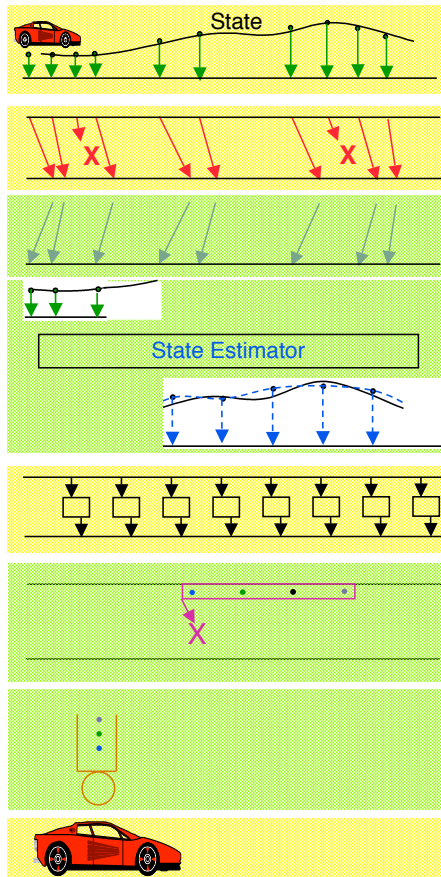
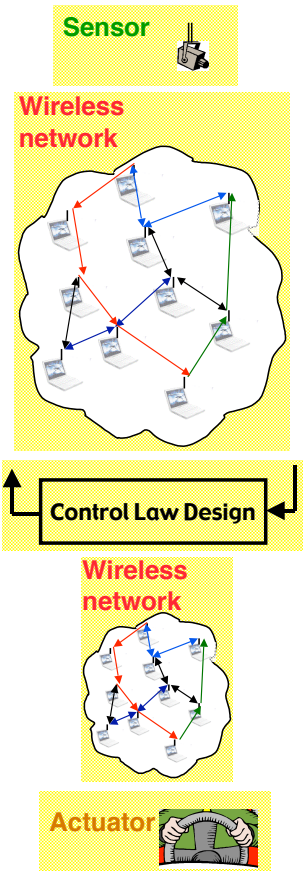


Time Translation Service

State Estimator

Receding Horizon Control

Actuator Buffer

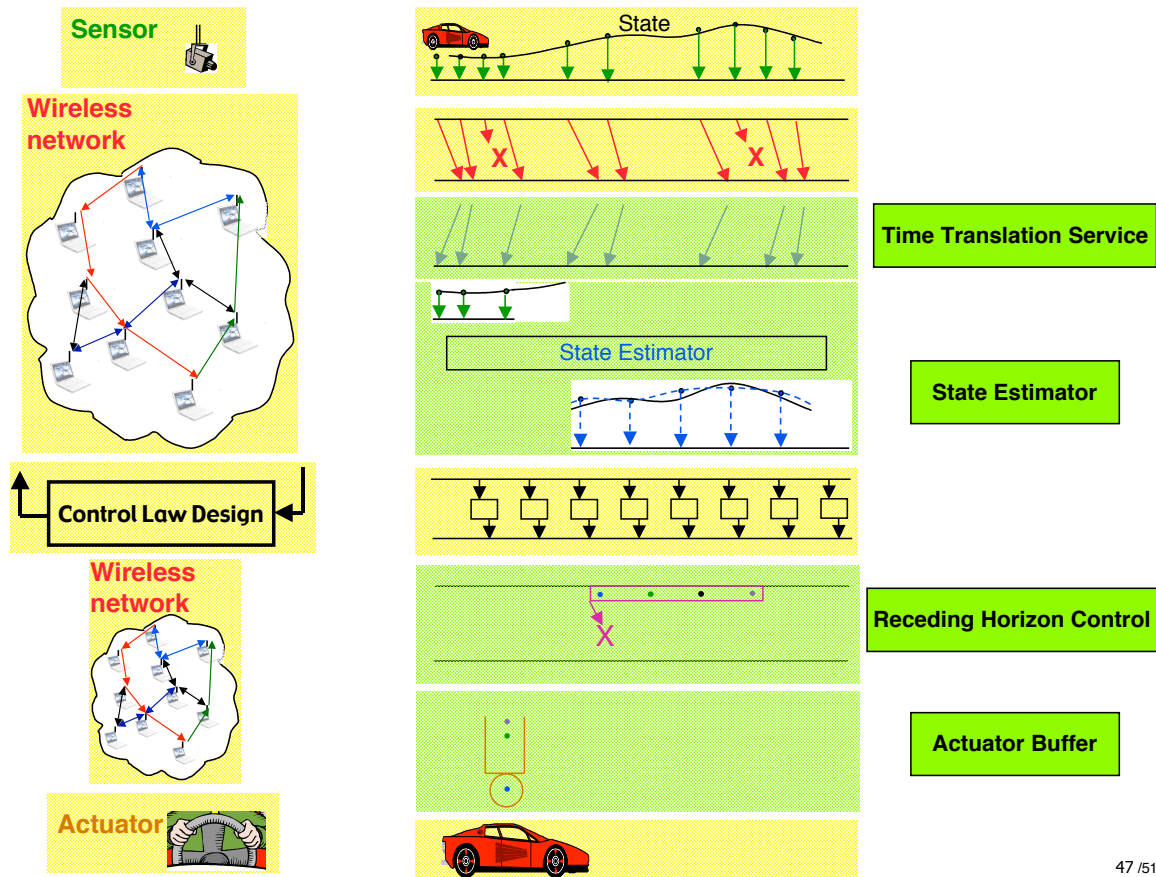


Time Translation Service

State Estimator

Receding Horizon Control

Actuator Buffer



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Local Temporal Autonomy

- ◆ Components able to tolerate failures of other components for some time
- ◆ Example: Insulating Controller from Sensor and Communication Network



- ◆ Example: Insulating Actuator from Controller and Communication Network



- ◆ Converts *Dependency* relationships to *Use If Available* relationships
- ◆ Makes possible other facilities such as

- Automatic Restart of Failed Components
- Migration of Components
- Component Upgrade at Runtime

Reliability, robustness
System integration, Initialization
Evolution and Scalability

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The oncoming theoretical convergence

Post Maxwell,
von Neumann,
Shannon,
Bardeen-Brattain world

- ◆ Sensor/Actuator networks
 - Nodes can compute
 - Nodes can communicate
 - Nodes can actuate
 - Nodes can sense

- ◆ 1950 — 2000 and continuing: Substantial progress in several individual disciplines
 - Computation: ENIAC (1946), von Neumann (1944), Turing,...
 - Sensing and inference: Fisher, Wiener (1949),...
 - Actuation/Control: Bode, Kalman (1960),...
 - Communication: Shannon (1948), Nyquist,...
 - Signal Processing: FFT, Cooley-Tukey (1965),...



- ◆ Larger grand unification of sensing, actuation, communication and computation
- ◆ ~ 2000 — onwards
 - A gradual fusion of all these fields
 - But still knowledge of all these fields may be important

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To obtain papers

- ◆ Papers can be downloaded from

<http://black.csl.uiuc.edu/~prkumar>

- ◆ For hard copies send email to

prkumar@uiuc.edu

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